

<div style="border: 2px solid black; padding: 5px; display: inline-block;">be-OI 2022</div> Finale - CADETS Saturday 23rd April 2022	Remplissez ce cadre en MAJUSCULES et LISIBLEMENT, svp PRÉNOM : NOM : ÉCOLE :	751 Réservé
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Finals of the Belgian Informatics Olympiad 2022 (time allowed : 2h maximum)

General information (read carefully before attempting the questions)

1. Verify that you have received the correct set of questions (as mentioned above in the header):
 - for the students in the second year of the Belgian secondary school system or below (US grade 8, UK year 9): category **cadets**.
 - for the students in the third or fourth year of the Belgian secondary school system or equivalent (US grade 9-10, UK year 10-11): category **junior**.
 - for the students in the fifth year of the Belgian secondary school system or equivalent (US grade 11, UK year 12) and above: category **senior**.
2. Write your first name (PRÉNOM), first name (NOM) and school (ÉCOLE) **on the first page only**.
3. Write **your answers** on the provided answer sheets, which you will find **at the end of the booklet**.
4. If you have to write outside the answer boxes due to a mistake, then continue writing **on the same sheet of paper**.
5. Write **clearly and legibly** with a blue or black **pen or ballpoint**.
6. You may only have writing materials with you. Calculator, GSM, ... are **forbidden**.
7. You can always request extra scratch paper from the invigilator.
8. When you have finished, **hand in this first page (with your name on it), and the pages with your answers**. You can keep the other pages.
9. All the snippets of code in the exercises are written in **pseudo-code**. On the next pages you will find a description of the pseudo-code that we use.
10. If you have to respond with code, you can do so in **pseudo-code** or in any **current programming language** (such as Java, C, C ++, Pascal, Python, ...). We do not deduct points for syntax errors.

Good Luck !

The Belgian IT Olympiad is possible thanks to the support from our members:



Pseudo-code checklist

Data is stored in variables. We change the value of a variable using \leftarrow . In a variable, we can store whole numbers, real numbers, or arrays (see below), as well as Boolean (logical) values: true/correct (**true**) or false/wrong (**false**). It is possible to perform arithmetic operations on variables. In addition to the four conventional operators (+, -, \times and /), you can also use the operator %. If a and b are whole numbers, then a/b and $a\%b$ denote respectively the quotient and the remainder of the division. For example, if $a = 14$ and $b = 3$, then $a/b = 4$ and $a\%b = 2$.

Here is a first code example, in which the variable *age* receives 17.

```
birthYear  $\leftarrow$  2003  
age  $\leftarrow$  2020 - birthYear
```

To run code only if a certain condition is true, we use the instruction **if** and possibly the instruction **else** to execute another code if the condition is false. The next example checks if a person is of legal age and stores the price of their movie ticket in the variable *price*. Note the comments in the code.

```
if (age  $\geq$  18)  
{  
    price  $\leftarrow$  8 // This is a comment.  
}  
else  
{  
    price  $\leftarrow$  6 // cheaper !  
}
```

Sometimes when one condition is false, we have to check another. For this we can use **else if**, which comes down to executing another **if** inside the **else** of the first **if**. In the following example, there are 3 age categories that correspond to 3 different prices for the movie ticket.

```
if (age  $\geq$  18)  
{  
    price  $\leftarrow$  8 // Price for a person of legal age (adult).  
}  
else if (age  $\geq$  6)  
{  
    price  $\leftarrow$  6 // Price for children aged 6 or older.  
}  
else  
{  
    price  $\leftarrow$  0 // Free for children under 6.  
}
```

To handle several elements with a single variable, we use an array. The individual elements of an array are identified by an index (which is written in square brackets after the name of the array). The first element of an array *tab* has index 0 and is denoted $tab[0]$. The second element has index 1 and the last has index $N - 1$ if the array contains N elements. For example, if the array *tab* contains the 3 numbers 5, 9 and 12 (in this order), then $tab[0] = 5$, $tab[1] = 9$, $tab[2] = 12$. The array is size 3, but the highest index is 2.

To repeat code, for example to browse the elements of an array, we can use a **for** loop. The notation **for** ($i \leftarrow a$ **to** b **step** k) represents a loop which will be repeated as long as $i \leq b$, in which i begins with the value a , and is increased by k at the end of each step. The following example calculates the sum of the elements of the array tab assuming its size is N . The sum is found in the variable sum at the end of the execution of the algorithm.

```
sum ← 0
for (i ← 0 to N - 1 step 1)
{
    sum ← sum + tab[i]
}
```

You can also write a loop using the instruction **while**, which repeats code as long as its condition is true. In the next example, we're going to divide a positive integer N by 2, then by 3, then by 4 ... until it is a single digit number (i.e. until $N < 10$).

```
d ← 2
while (N ≥ 10)
{
    N ← N/d
    d ← d + 1
}
```

Often the algorithms will be in a frame and preceded by descriptions. After **Input**, we define each of the arguments (variables) given as input to the algorithm. After **Output**, we define the state of certain variables at the end of the algorithm execution and possibly the returned value. A value can be returned with the instruction **return**. When this instruction is executed, the algorithm stops and the given value is returned.

Here is an example using the calculation of the sum of the elements of an array.

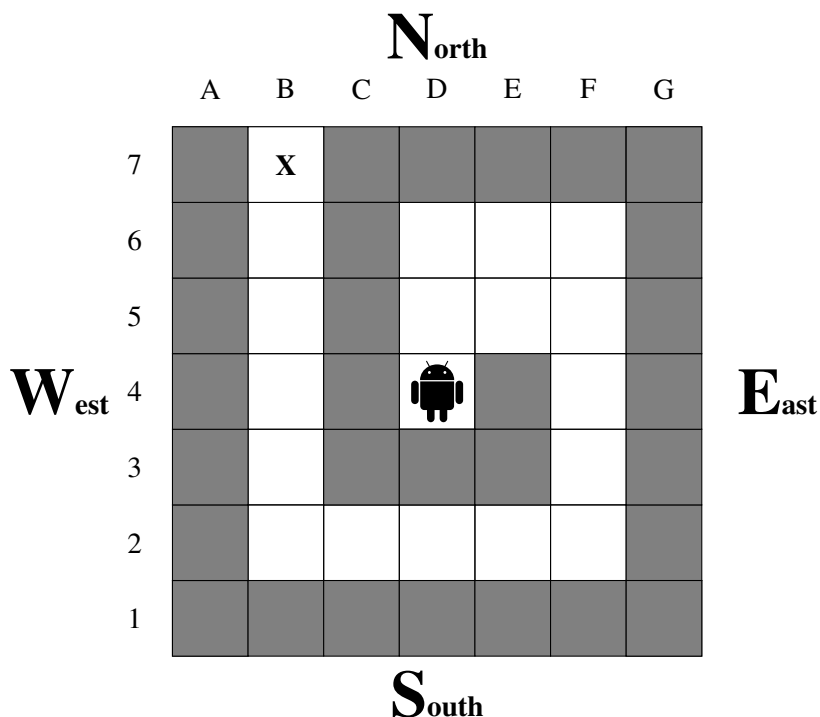
```
Input : tab, an array of N numbers.
        N, the number of elements in the array.
Output : sum, the sum of all the numbers in the array.

sum ← 0
for (i ← 0 to N - 1 step 1)
{
    sum ← sum + tab[i]
}
return sum
```

Note: in this last example, the variable i is only used as a counter for the **for** loop. There is therefore no description for it either in **Input** or in **Output**, and its value is not returned.

Question 1 – Nono the little robot

Nono, the little robot, is stuck in the middle of a labyrinth.



Nono can move along the white squares but cannot land on grey squares, which represent walls. In the beginning, Nono stands in the middle of the labyrinth on the square with coordinates **D4**. Nono has to reach the exit: the square with coordinates **B7** marked with a **X**.

Nono moves one square at a time with the command `Go()`, which receives one of the following parameters: N, S, E ou W. Every parameter corresponds to one of the four cardinal points which are shown on the picture above, with North at the top according to the usual convention.

On the following page, we propose several algorithms to get Nono out of the maze. We want to know if Nono is on the square **X** at the end of the execution of each programs or if he collides with a wall (and, in this case, we ask the coordinates of the wall with which the collision takes place).

Some algorithms use arrays. For example `Dir ← [N, E, S, W, N]` in algorithm 4 initialises an array with 5 elements, which are `Dir[0]=N, Dir[1]=E, Dir[2]=S, Dir[3]=W` and `Dir[4]=N`.

Algorithm 1

```

Go(N)
for (i ← 1 to 2 step 1)
{
  Go(E)
}
for (i ← 1 to 3 step 1)
{
  Go(S)
}
for (i ← 1 to 4 step 1)
{
  Go(W)
}
for (i ← 1 to 5 step 1)
{
  Go(N)
}

```

Algorithm 2

```

Go(N)
i ← 1
while (i ≤ 2)
{
  Go(E)
  i ← i+1
}
while (i ≥ 0)
{
  Go(S)
  i ← i-1
}
while (i ≤ 4)
{
  Go(W)
  i ← i+1
}
i ← 0
while (i < 5)
{
  Go(N)
  i ← i+1
}

```

Algorithm 3

```

Go(N)
j ← 2
for (i ← 1 to j step 1)
{
  Go(E)
}
j ← j+1
for (i ← 1 to j step 1)
{
  Go(S)
}
j ← j+1
for (i ← 1 to j step 1)
{
  Go(W)
}
j ← j+1
for (i ← 1 to j step 1)
{
  Go(N)
}

```

Algorithm 4

```

Dir ← [N,E,S,W,N]
Stp ← [1,2,3,4,5]
for (j ← 0 to 4 step 1)
{
  for (i ← 1 to Stp[j] step 1)
  {
    Go(Dir[j])
  }
}

```

Algorithm 5

```

Dir ← [N,E,W,E,S,N,S,W,E,W,N]
Stp ← [1,2,1,1,2,1,2,4,2,1,5]
for (j ← 0 to 10 step 1)
{
  for (i ← 1 to Stp[j] step 1)
  {
    Go(Dir[j])
  }
}

```

Q1(a) [5 pts]	Does algorithm 1 bring Nono onto the square X ? If your answer is « no » and Nono collides with a wall, also provide the coordinates of the first wall that Nono collides with.
Q1(b) [5 pts]	Does algorithm 2 bring Nono onto the square X ? If your answer is « no » and Nono collides with a wall, also provide the coordinates of the first wall that Nono collides with.
Q1(c) [5 pts]	Does algorithm 3 bring Nono onto the square X ? If your answer is « no » and Nono collides with a wall, also provide the coordinates of the first wall that Nono collides with.
Q1(d) [5 pts]	Does algorithm 4 bring Nono onto the square X ? If your answer is « no » and Nono collides with a wall, also provide the coordinates of the first wall that Nono collides with.
Q1(e) [5 pts]	Does algorithm 5 bring Nono onto the square X ? If your answer is « no » and Nono collides with a wall, also provide the coordinates of the first wall that Nono collides with.

Question 2 – Peak positions

Given an array $a[]$ of n numbers, a *peak position* of $a[]$ is a position i in that array such that $a[i]$ is at least as large as both the element to its left and the element to its right (if they exist). Note that arrays are 0-indexed: the first element is at position 0 and the last element is at position $n - 1$.

For example, if $a = [2, 7, 4, 5]$, then the peak positions of $a[]$ are the positions 1 and 3 (corresponding to the values 7 and 5). On the other hand, if $a = [6, 6, 6]$, then all the positions (0, 1 and 2) are peak positions. It is easy to show that any array has at least one peak position.

Q2(a) [1 pt] Give *all* the peak positions of array $a = [1, 2, 3, 2, 1]$.

Q2(b) [1 pt] Give *all* the peak positions of array $a = [5, 4, 3, 2, 1]$.

Q2(c) [2 pts] Give *all* the peak positions of array $a = [4, 2, 5, 3]$.

Q2(d) [2 pts] Give *all* the peak positions of array $a = [0, 10, 10, 0, 0]$.

There are quite a few ways to find a peak position, but it is very easy to make mistakes! Your friend Alex sent you the following program listings last night at 3am. He claims that his programs can find a peak position of any array $a[]$. You figure that Alex was probably very tired when writing the programs and you decide to check them.

It is assumed that in each program, the array of numbers $a[]$ has $n \geq 2$ elements.

Program 1:

```

for (i ← 1 to n-2 step 1)
{
    if (a[i] >= a[i-1] and a[i] >= a[i+1])
    {
        return i
    }
}
if (a[0] > a[n-1])
{
    return 0
}
else
{
    return n-1
}

```

Q2(e) [1 pt] What value does program 1 return if $a = [9, 8, 7, 6, 5]$?

Q2(f) [1 pt] What value does program 1 return if $a = [0, 1, 3, 4]$?

Q2(g) [1 pt] What value does program 1 return if $a = [0, 0, 0, 0]$?

Q2(h) [1 pt] What value does program 1 return if $a = [1, 0, 0, 1]$?

Q2(i) [2 pts] Does program 1 return a peak position for any array $a[]$?

Program 2:

```
i ← 0
for (j ← 1 to n-1 step 1)
{
    if (a[j] > a[i])
    {
        i ← j
    }
}
return i
```

Q2(j) [1 pt] What value does program 2 return if $a = [4, 3, 2, 1]$?

Q2(k) [1 pt] What value does program 2 return if $a = [0, 1, 0, 5, 0, 5, 0]$?

Q2(l) [2 pts] Does program 2 return a peak position for any array $a[]$?

Program 3:

```
if (a[0] > a[n-1])
{
    return 0
}
else
{
    return n-1
}
```

Q2(m) [1 pt] What value does program 3 return if $a = [1, 2, 3]$?

Q2(n) [1 pt] What value does program 3 return if $a = [2, 2, 1]$?

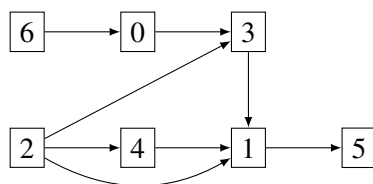
Q2(o) [1 pt] What value does program 3 return if $a = [1, 2, 3, 2, 1]$?

Q2(p) [2 pts] Does program 3 return a peak position for any array $a[]$?

Question 3 – The computer factory

The company be-OI father and son manufactures computer parts. A computer component is a complex object and requires, to be manufactured, other components, which are themselves assembled from other components, *etc.* The company has all the machines to manufacture everything, but cannot make them all work at the same time. So it has to find *the right order to make the parts, assuming that each machine will only be operated once.*

Each machine has a number from 0 to $n - 1$ and the company has represented the dependencies between the machines using a diagram as shown in the following example.



On this diagram, each machine is represented by a rectangle with the machine number. An arrow going from machine i to machine j means that machine i must run before machine j , because the parts produced by i are necessary for those produced by j (we don't care about the quantities here: it is enough for i to run only once to allow j to run). For example, it is mandatory to run machine 2 and machine 0 before machine 3. Any operating order of the machines where 3 is run before 2 or before 0 is therefore impossible. In order for the diagram to make sense, we assume that it never contains a *cycle*, i.e. that it is never possible to start from a machine and follow a series of arrows to return to the same machine.

As you can see, some machines can be started up immediately.

Q3(a) [1 pt]	According to the diagram above, what are all the machines can be started immediately?
---------------------	--

Q3(b) [1 pt]	According to the diagram above, what are all the machines that can be started if only machine 2 has been run (remember: each machine is only run once) ?
---------------------	---

Which of the following orders of operating the machines are possible within the constraints given in the above diagram ?

		Order of operating the machines
Q3(c) [1 pt]	Possible / Impossible	0,1,2,3,4,5,6
Q3(d) [1 pt]	Possible / Impossible	6,0,2,3,4,1,5
Q3(e) [1 pt]	Possible / Impossible	6,5,4,3,2,1,0
Q3(f) [1 pt]	Possible / Impossible	2,4,6,0,3,1,5
Q3(g) [1 pt]	Possible / Impossible	2,4,1,6,0,3,5

Clearly, there is a very specific condition that the machines must meet (in a diagram like the one above) so that we can make them work immediately.



Q3(h) [2 pts]	Among the propositions below, which specifically characterizes the machines that can be operated immediately?
<input type="checkbox"/>	Those machines that have an even number of incoming arrows.
<input type="checkbox"/>	Those machines that have at most 2 incoming arrows.
<input type="checkbox"/>	Those machines that have no incoming arrows.
<input type="checkbox"/>	Those machines that have at least one incoming arrow.
<input type="checkbox"/>	Those machines that have no incoming arrows and an even (machine) number.

We are now looking for an algorithm to find an order to operate the machines, which is compatible with the diagram. The diagram is given as a matrix of Booleans $M[n][n]$, where $M[i][j]$ is equal to **true** if and only if there is an arrow going from machine i to machine j .

Here is the matrix for the example diagram.
Boxes with a value of **true** have been highlighted to improve readability.

	0	1	2	3	4	5	6
0	false	false	false	true	false	false	false
1	false	false	false	false	false	true	false
2	false	true	false	true	true	false	false
3	false	true	false	false	false	false	false
4	false	true	false	false	false	false	false
5	false	false	false	false	false	false	false
6	true	false	false	false	false	false	false

M[][]

$M[2][4]$ is surrounded by a solid line, while $M[4][2]$ is surrounded by a dotted line.

$M[2][4] = \mathbf{true}$ because there is an arrow going from machine 2 to machine 4.

$M[4][2] = \mathbf{false}$ because there is no arrow going from machine 4 to machine 2.

The proposed algorithm is based on a data structure called *queue*. It is a queue, with a beginning and an end. We add the elements at the end of the queue and we process the elements starting with the one at the beginning of the queue. We have the functions: `Empty()`, which empties the queue (it no longer contains any elements); `Insert(v)`, which adds the element v to the **end** of the queue; `Remove()`, which returns the element of the **start** of the queue and removes it from the queue; and finally `IsEmpty()` which returns **true** if the queue is empty and **false** if it contains at least one element.

The algorithm is the following

1. We start by inserting into the queue all the machines that we can immediately start running.
2. Then we repeat the same actions until the queue is empty:
 - (a) take a machine at the beginning of the queue and run the machine;
 - (b) if operating this machine makes it possible for other machines to start running, add these new machines to the queue.

Remarks.

A boolean value `bool` can be used directly in an instruction `if (bool) { ... }`.

The `not` operator acts as follows on Boolean values: `not true` is equal to `false` and `not false` is equal to `true`.

Here is an implementation of the algorithm:

Input : A matrix $M[n][n]$ of size $n \times n$, which represents the dependencies between the n machines.

Output : Runs the machines in an order compatible with M .

```

Empty()
D ← [0,...,0] // (an array of length n, initialized with all elements equal to 0)

for (j ← 0 to n-1 step 1)
{
  for (i ← 0 to n-1 step 1)
  {
    if (M[i][j])
    {
      D[j] ← D[j] + 1
    }
  }
  if (D[j] = 0)
  {
    Insert(j)
  }
}

while (not IsEmpty())
{
  m ← Remove()
  Operating the machine m
  for (i ← 0 to n-1 step 1)
  {
    if (M[m][i])
    {
      D[i] ← D[i] - 1
      if (D[i] = 0)
      {
        Insert(i)
      }
    }
  }
}

```

Q3(i) [3 pts]

In which order will the algorithm make the machines run ?

Question 4 – LIDAR

LIDAR is a technology that uses light or lasers to determine distances or heights of objects. You are part of a team that wants to map out how high exactly different parts of the Great Wall of China are. While flying high above the Wall, you suddenly notice that your LIDAR equipment has a problem: instead of measuring the height of a single segment, it measures and sums together the heights of several consecutive segments. You only had permission to fly over the Wall today, and there is no time to go back to reconfigure the LIDAR. As you are the algorithmic expert of the team, your colleagues look to you to recover the actual heights of the segments from the data gathered in the scan.

For simplicity, we represent the Wall as a list $W[]$ of n positive or null integers ($W[i] \geq 0$).

Each $W[i]$ is the height of a segment of the Wall.

The LIDAR will take q scans, each will be the sum of consecutive elements of $W[]$.

Example: take for instance a wall with $n = 4$ segments: $W = [4, 3, 5, 8]$.

As usual the index start at 0, so here $W[0] = 4$, $W[1] = 3$, $W[2] = 5$ and $W[3] = 8$.

The results of 2 scans by the LIDAR could be (pay attention to the notation $W[i \dots j] = W[i] + \dots + W[j]$):

$W[1 \dots 3] = W[1] + W[2] + W[3] = 3 + 5 + 8 = 16$ and $W[0 \dots 1] = W[0] + W[1] = 4 + 3 = 7$.

For the following four questions, consider a wall $W[]$ with 4 segments.

The LIDAR has measured $W[0 \dots 2] = 31$, $W[0 \dots 3] = 42$ and $W[2 \dots 3] = 17$.

Q4(a) [1 pt]	How high is $W[3]$?
---------------------	--

Q4(b) [1 pt]	How high is $W[2]$?
---------------------	--

Q4(c) [1 pt]	What is the value of $W[0 \dots 1]$?
---------------------	---

Q4(d) [1 pt]	How many different walls are compatible with the LIDAR measurements ?
---------------------	--

Before solving the real problem, we first try to simulate the measurements effectively. This will allow us to generate test cases to check whether we have done things correctly.

Let's first implement a simple, but slow algorithm. The inputs are the wall $W[]$ and its length n , the number of scans q , and the left and right endpoints for the scans in the tables $left[]$ and $right[]$. The output is an array $Lidar[]$ whose elements are the sums $W[left[i] \dots right[i]]$ measured by the scans.

```

Input : n, W[], q, left[], right[]
Output : Lidar[]

Lidar[] is initialized to q zeroes.

for (i ← 0 to ... step 1) // (i)
{
    for (j ← left[i] to ... step 1) // (ii)
    {
        Lidar[i] ← Lidar[i] + ... // (iii)
    }
}

```

There are a few blanks in this implementation, can you fill them in?

Q4(e) [1 pt]	What is expression (i) in the above algorithm ?
---------------------	--

Q4(f) [1 pt]	What is expression (ii) in the above algorithm ?
---------------------	---

Q4(g) [1 pt]	What is expression (iii) in the above algorithm ?
---------------------	--

Here is a faster algorithm, with only a single pass over both the values of $W[]$ and of $left[]$ and $right[]$. The idea is to preprocess a prefix table $P[]$ such that $P[0] = 0$ and $P[i + 1] = W[0 \dots i]$ and then use it to calculate $Lidar[]$. The inputs and output are the same as in the first algorithm.

```

Input  : n, W[], q, left[], right[]
Output : Lidar[]

P[] ← [0,0,---,0] //n+1 "0".

for (i ← 0 to ... step 1) // (i)
{
    P[i + 1] ← ... // (ii)
}

for (i ← 0 to ... step 1) // (iii)
{
    Lidar[i] ← ... // (iv)
}

```

You just have to fill in a few blanks. Make sure you pay close attention to the indices you use.

Q4(h) [1 pt]	What is expression (i) in the above algorithm ?
---------------------	--

Q4(i) [2 pts]	What is expression (ii) in the above algorithm ?
----------------------	---

Q4(j) [1 pt]	What is expression (iii) in the above algorithm ?
---------------------	--

Q4(k) [3 pts]	What is expression (iv) in the above algorithm ?
----------------------	---

It seems like we got a bit lucky, and all of our scans are the values $W[0 \dots \text{right}[i]]$, so we actually have the value of the preprocessing table $P[]$ from the previous algorithm. This means we just need to undo that preprocessing to get back the heights of the individual segments of the wall $W[]$. The inputs are the number of segments n in the wall, and the prefix array $P[]$ such that $P[0] = 0$ and $P[i + 1] = W[0 \dots i]$. The output is the wall $W[]$.

```
Input  : n, P[]
Output : W[]

for (i ← ... to ... step 1) // (i), (ii)
{
    W[i] ← ... // (iii)
}
```

Can you fill in the blanks ?

Q4(l) [1 pt]	What is expression (i) in the above algorithm ?
Q4(m) [1 pt]	What is expression (ii) in the above algorithm ?
Q4(n) [2 pts]	What is expression (iii) in the above algorithm ?

Question 5 – Binaïro

Binaïro alias **Takuzu** is a logic game with simple rules but complex solutions.

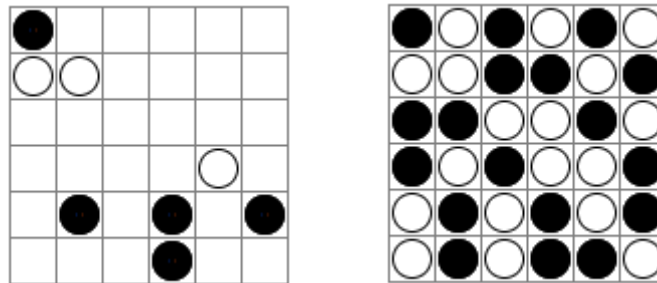
The game is played on a square grid of even size ($2n$ rows of $2n$ cells).

At the start, some cells contain a piece, black or white. All other cells are empty.

The goal is to put a piece in each cell according to the following rules.

- **Rule 1:** Each row or column must contain n white pieces and n black pieces.
- **Rule 2:** In each row or column, you can have two consecutive pieces of the same color, but not three.
- **Rule 3:** Each row and each column is unique (we won't need this rule in what comes next).

Here is an example of a 6x6 binaïro grid (left) and the unique solution (right).



Below are 2 examples of rows that do not respect the rules.



Rule 1 not respected (there are more white pieces than black ones).



Rule 2 not respected (there are more than 2 consecutive black pieces).

Complete the following rows **while respecting the first 2 rules**.

If necessary, answer here in draft form before **copying to the answer sheet**.

Q5(a) [1 pt]	Complete the row
--------------	------------------

Q5(b) [1 pt]	Complete the row
--------------	------------------

Q5(c) [1 pt]	Complete the row
--------------	------------------

In how many ways can the following rows be completed **while respecting the first 2 rules** ?

Q5(d) [1 pt]	Number of ways to complete
--------------	----------------------------

Q5(e) [1 pt]	Number of ways to complete
--------------	----------------------------

Q5(f) [1 pt]	Number of ways to complete
--------------	----------------------------






Q5(g) [1 pt]	Number of ways to complete <input type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input checked="" type="radio"/> <input type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input checked="" type="radio"/>
Q5(h) [1 pt]	Number of ways to complete <input type="radio"/> <input type="radio"/> <input checked="" type="radio"/> <input type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>
Q5(i) [1 pt]	Number of ways to complete <input type="radio"/> <input type="checkbox"/> <input type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input type="radio"/>
Q5(j) [1 pt]	Number of ways to complete <input type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input type="radio"/>
Q5(k) [1 pt]	Number of ways to complete <input checked="" type="radio"/> <input type="checkbox"/> <input type="checkbox"/> <input type="radio"/> <input type="radio"/> <input checked="" type="radio"/> <input type="checkbox"/> <input type="radio"/> <input checked="" type="radio"/>
Q5(l) [1 pt]	Number of ways to complete <input type="checkbox"/> <input type="checkbox"/>
Q5(m) [1 pt]	Number of ways to complete <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>

The **program 1** checks if a row of black and white pieces respects the first 2 rules. Some parts of the code are missing, they must be completed.

The row to check is represented by an array of integers $binairo[]$. White pieces are represented by 1 and black pieces by 2. A number n is also given: the array $binairo[]$ contains $2n$ elements (numbered from 0 to $2n - 1$) and according to **Rule 1**, there must be the same number n of white and black pieces. The program must return **true** if the first two rules are respected and **false** otherwise.

Examples.

- For  $n = 5$, $binairo = [2, 1, 1, 2, 1, 2, 1, 2, 2, 1]$, the program returns **true**.
- For  $n = 3$, $binairo = [1, 2, 2, 2, 1, 1]$, the program returns **false**.
- For  $n = 4$, $binairo = [2, 1, 2, 2, 1, 2, 1, 2]$, the program returns **false**.

The program traverses $binairo[]$ and uses the variable $t1$ to count the **total** number of white pieces and the variable $c1$ to count the number of **consecutive** white pieces among the last ones scanned. The variables $t2$ and $c2$ do the same for the black pieces.

Program 1:

```

Input  : n, binairo[]
Output : true/false
t1 ← 0; t2 ← 0; c1 ← 0; c2 ← 0
for (i ← 0 to 2*n-1 step 1){
    if (binairo[i] = 1) {
        t1 ← ...
        if (t1 > ...) {return false}
        c1 ← ...
        if (c1 = ...) {return false}
        c2 ← ...
    }
    else {
        t2 ← ...
        if (t2 > ...) {return false}
        c2 ← ...
        if (c2 = ...) {return false}
        c1 ← ...
    }
}
return ...

```

You can fill in the code above in draft form but don't forget to **copy on the answer sheet**.

Q5(n) [6 pts]

Complete the ... in program 1.

Score between 0 and 6. You lose 1 point for each mistake.

Donnez vos réponses ici !

Q1(a)	Yes or No and coordinates of the collision if applicable.	/5
Q1(b)	Yes or No and coordinates of the collision if applicable.	/5
Q1(c)	Yes or No and coordinates of the collision if applicable.	/5
Q1(d)	Yes or No and coordinates of the collision if applicable.	/5
Q1(e)	Yes or No and coordinates of the collision if applicable.	/5
Q2(a)	A list of <i>positions</i> in array $a[]$ (each between 0 and 4)	/1
Q2(b)	A list of <i>positions</i> in array $a[]$ (each between 0 and 4)	/1
Q2(c)	A list of <i>positions</i> in array $a[]$ (each between 0 and 3)	/2
Q2(d)	A list of <i>positions</i> in array $a[]$ (each between 0 and 4)	/2
Q2(e)	An integer	/1
Q2(f)	An integer	/1
Q2(g)	An integer	/1
Q2(h)	An integer	/1
Q2(i)	Yes or No	/2

Q2(j)			An integer	/1
Q2(k)			An integer	/1
Q2(l)			Yes or No	/2
Q2(m)			An integer	/1
Q2(n)			An integer	/1
Q2(o)			An integer	/1
Q2(p)			Yes or No	/2
Q3(a)			One or more machine numbers	/1
Q3(b)			One or more machine numbers	/1
	Possible	Impossible	Order of operating the machines	/5
Q3(c) /1	<input type="checkbox"/>	<input type="checkbox"/>	0,1,2,3,4,5,6	
Q3(d) /1	<input type="checkbox"/>	<input type="checkbox"/>	6,0,2,3,4,1,5	
Q3(e) /1	<input type="checkbox"/>	<input type="checkbox"/>	6,5,4,3,2,1,0	
Q3(f) /1	<input type="checkbox"/>	<input type="checkbox"/>	2,4,6,0,3,1,5	
Q3(g) /1	<input type="checkbox"/>	<input type="checkbox"/>	2,4,1,6,0,3,5	
Q3(h)	Ne cochez qu'UNE seule réponse !			/2
<input type="checkbox"/>	Those machines that have an even number of incoming arrows.			
<input type="checkbox"/>	Those machines that have at most 2 incoming arrows.			
<input type="checkbox"/>	Those machines that have no incoming arrows.			
<input type="checkbox"/>	Those machines that have at least one incoming arrow.			
<input type="checkbox"/>	Those machines that have no incoming arrows and an even (machine) number.			

Q3(i)	A sequence of machine numbers	/3
Q4(a)	The height $W[3]$	/1
Q4(b)	The height $W[2]$	/1
Q4(c)	The value of $W[0 \dots 1]$	/1
Q4(d)	A number	/1
Q4(e)	The expression (i)	/1
Q4(f)	The expression (ii)	/1
Q4(g)	The expression (iii)	/1
Q4(h)	The expression (i)	/1
Q4(i)	The expression (ii)	/2
Q4(j)	The expression (iii)	/1
Q4(k)	The expression (iv)	/3
Q4(l)	The expression (i)	/1
Q4(m)	The expression (ii)	/1
Q4(n)	The expression (iii)	/2

Q5(n)

Complete the ... in program 1.

/6

```
Input : n, binaire[]
Output : true/false
t1 ← 0; t2 ← 0; c1 ← 0; c2 ← 0
for (i ← 0 to 2*n-1 step 1){
  if (binaire[i] = 1) {
    t1 ← .....
    if (t1 > ..... ) {return false}
    c1 ← .....
    if (c1 = ..... ) {return false}
    c2 ← .....
  }
  else {
    t2 ← .....
    if (t2 > ..... ) {return false}
    c2 ← .....
    if (c2 = ..... ) {return false}
    c1 ← .....
  }
}
return .....
```